

# Formal Theory & Causality

## Lecture 5 – Part II

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Exp Class Lectures

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- What do we learn from such experiments?

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- Stress tests very important ways in which to evaluate robustness of theory & results

# FTA & the Analysis Stage

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  - examples – relationship between subjects' cognitive behavioral differences, the influence of altruism or views of fairness or reciprocity, & how subjects learn & manipulations.
- A larger number of FTA experiments are being conducted in the field where control is less easily maintained & random assignment can be problematic

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- Lots of way do this, discuss one example.



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- Could these variations in subjects' choices be a consequence of errors that subjects make in translating their preferences into choices?
- Consider the centipede Game

# FTA & the Analysis Stage

## The Centipede Game & Strategic Errors

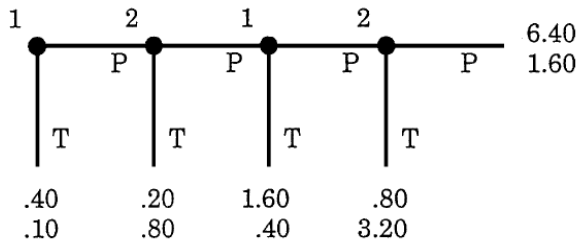


Figure: The Centipede Game from McKelvey and Palfrey (1992)

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- Key assumption actors' deviations from optimal decisions are negatively correlated with the associated costs and that in equilibrium players' beliefs about these deviations match the equilibrium choice probabilities.



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- Key assumption actors' deviations from optimal decisions are negatively correlated with the associated costs and that in equilibrium players' beliefs about these deviations match the equilibrium choice probabilities.
- Goeree, Holt, and Palfrey (2008) provide an axiomatic definition of what they label *Regular* QRE and they demonstrate that given these axioms regular QRE exist in normal form games.

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## Quantal Response Equilibrium

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- $\sigma_{ij} = \frac{e^{\lambda U_{ij}(\sigma)}}{\sum_{k \in S_i} e^{\lambda U_{ik}(\sigma)}}$  for all  $i, j \in S_i$  where  $\sigma_{ij}$  is the probability  $i$  chooses strategy  $j$  &  $U_{ij}(\sigma)$  is the equilibrium expected payoff to  $i$  if  $i$  chooses decision  $j$  and the players in the game have a strategy profile of  $\sigma$ .

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- A higher  $\lambda$  reflects a less noisy response to the payoffs. In the extreme, when  $\lambda = 0$  subjects are choosing purely randomly and when  $\lambda = +\infty$  subjects are choosing according to the Nash equilibrium.

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- Alternatively, can across data sets or work directly from the axioms of regular QRE which imposes empirical restrictions.
- **However, criticism exemplifies importance of assumptions made about stochastic processes when creating a theoretically derived structural model for empirical evaluation.**

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# FTA, Field Experiments, & Observational Data

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- Example of survey experiment – Tomz & VH

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- Examples with nonexperimental data – Coate & Conlin & others